

2013

SIGNAL & SYSTEM

Time Allotted : 3 Hours

Full Marks : 70

The figures in the margin indicate full marks.

Candidates are required to give their answers in their own words

as far as practicable.

GROUP - A

(Multiple Choice Type Question)

1. Choose the correct alternatives for any *ten* of the following:

10 x 1 = 10

i) Laplace Transform of e^{-at} is

a) $\frac{1}{(s+a)}$

b) $\frac{1}{(s-a)}$

b) $\frac{a}{(s-a)}$

d) $\frac{a}{(s-a)}$

ii) $x(t)=a\sin\omega t$ is an

a) odd signal

b) even signal

c) both (a) and (b)

d) either (a) or (b).

iii) The signal $x(n)= 1+ e^{j4\pi n/7} - e^{j2\pi n/5}$ is periodic with period of

a) $\frac{5}{7}$

b) $\frac{7}{5}$

c) $\frac{4}{7}$

d) $\frac{4}{5}$

iv) The system define as $y(n)=2x(n)+3x(n^2)$ is

a)static , causal

b)dynamic ,causal

c)static ,non-causal

d)dynamic ,non-causal

v) ROC of unit step function is

a) $|z|<1$

b) $|z|>1$

c) $|z|=1$

d)none of these

vi) The discrete time system defined as

$$H(z)=\frac{z^3-3z^2+2z}{z^2+\frac{1}{2}z-\frac{1}{4}} \text{ is}$$

a)causal

b) non-causal

c)none of these

vii) Which one of the following rules determines the mapping of s-plane to z-plane

a) Right half of s-plane maps into outside of unit circle in z-plane.

b) Left half of s-plane maps into inside of unit circle in z-plane.

c) Imaginary axis of s-plane maps into circumference of unit circle in z-plane

d) All of these

viii) Energy of power signal is

- a) finite
- b) zero
- c) infinite
- d) between 1 and 2

ix) A system with input $x(n)$ & output $y(n)$ is given as

$$y(n) = \sin(5/6\pi n)x(n). \text{ The system is}$$

- a) Linear, stable & invariant
- b) Non-linear, stable & variant
- c) Linear, stable & variant
- d) Linear, unstable & invariant

x) The fourier transform of a conjugate symmetric function is

- a) imaginary
- b) real
- c) conjugate asymmetric
- d) conjugate symmetric

xi) Energy density function is always

- a) even
- b) odd
- c) neither even nor odd
- d) both (a) & (b)

xii) A discrete time system is stable if and only if the ROC of $H(z)$

- a) excludes $|z|=1$
- b) includes $|z|=1$
- c) both (a) & (b)
- d) none of these

GROUP - B
(Short Answer Type Questions)

Answer any *three* of the following.

3 x 5 = 15

2. What is meant by aliasing ? What is an anti-aliasing filter?

2+3

3. Explain the properties of $X(z)$.

4. What is time-invariant system? Determine whether the following

Signal is time- invariant or not :

2+3

$$Y(t)=x(-t)$$

5. State and prove initial value theorem of Z- transform

6. Determine the energy and power of the following signals:

a) $x(t)=t u(t)$

b) $x_2(n)=3e^{j3\pi n}$

3+2

GROUP - C

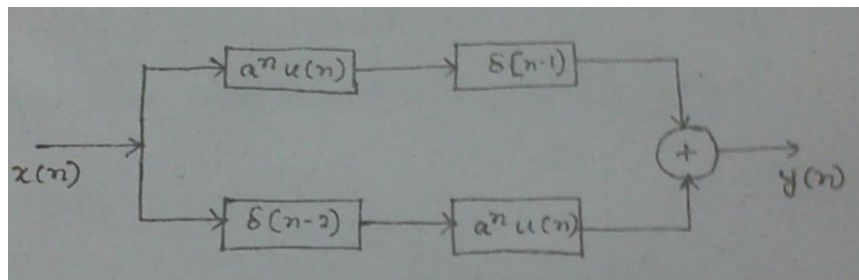
(Long Answer Type Questions)

Answer any three of the following.

3 x 15 = 45

7. a) LTI system can be completely characterized by its impulse response. Explain.

b) Find the overall impulse response of the system shown in fig:

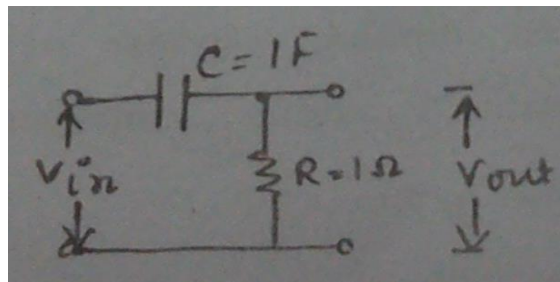


b) Using Z-transform find the convolution of two sequence

$$X_1(n)=\{1,2,-1,0,3\}; x_2(n)=\{1,2,-1\}$$

5+5+5

8. a) Find out the output of the system shown in figure given below for the input $e^{-2t} u(t)$ using laplace transform:



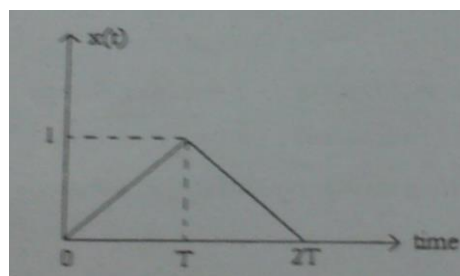
- c) Sketch the convolution of following two signals:

$$x(t) = \begin{cases} t+1, & 0 \leq t \leq 1 \\ 2-t, & 1 \leq t \leq 2 \\ 0, & \text{elsewhere} \end{cases}$$

and $h(t) = \delta(t+2) + 2\delta(t+1)$.

7+8

9. a) Define s-plane . Describe the concept of poles and zeros in complex plane.
 b) If $X(s)$ is the Laplace transform of $x(t)$, then show that $L[x(at)] = 1/|a| X(s/a)$.
 c) Determine Laplace transform of a given signal below:

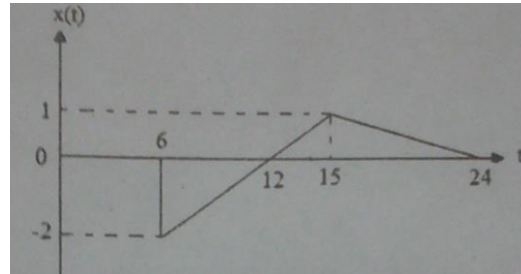


5+4+6

10. a) Sketch the given signal $x(t) = A[u(t+a) - u(t-a)]$ for $a > 0$. Also determine The given signal is a power signal or an energy signal or neither.
 b) From the given impulse response $h(n) = 5^n u(3 - n)$, check the causality & stability of the system.

c) What is half - wave symmetry?

d) The signal $x(t)$ is shown below:



6+4+1+4

Sketch signal $x(3t)$.

11. a) What is Z-transform ? Find inverse Z-transform of the following:

$$X(z) = \frac{(z+0.5)}{(z+0.6)(z+0.8)} \quad (\text{using Residue method}).$$

b) State the properties of ROC. (2+10)+3

12. Write short notes on any three of the following : 3*5

a) Dirichlet's condition for Fourier series

b) Time scaling of a signal

c) Causal system & non-causal system

d) Conditional probability

e) Scalar signal & vector signal.